

# Thermal Transient Computational Information

## Software Version 3.2

### 1. Acquired Data

| Symbol | Description  |
|--------|--|
| $V_n$  | acquired voltage samples, sampled and quantized $V(t)$ |
| $I_n$  | acquired current samples, sampled and quantized $I(t)$ |
| $t_n$  | acquired sample times                                  |

### 2. Thermal Transient Computation

| Symbol/Equation  | Description  |
|--|--|
| $R_n = V_n/I_n$  | sampled bridgewire resistance  |
| $V_{\text{corr}_n} = R_n * I_{\text{test}}$                        | corrected voltage, $I_{\text{test}}$ = requested test current  |
| $P_{VA}(), P_{IA}(), P_{RA}()$                                     | regression predictors for $V(t)$ , $I(t)$ and $R(t)$ computed over $R_A = [t_A, t_A + \Delta t_A]$                                       |
| $P_{VB}(), P_{IB}(), P_{RB}()$                                     | regression predictors for $V(t)$ , $I(t)$ and $R(t)$ computed over $R_B = [t_{\text{pulse}} - t_B - \Delta t_B, t_{\text{pulse}} - t_B]$ |
| $V_{\text{TR}} = P_{VB}(t_{\text{pulse}}) - P_{VA}(t_{\text{TR}})$ | Thermal Response voltage   |
| $R_0 = P_{RA}(t_{\text{start}})$                                   | initial (cold) resistance  |
| $\Delta R = P_{RB}(t_{\text{pulse}}) - P_{RA}(t_{\text{start}})$   | total change resistance. Note that the $\Delta R$ change in resistance does not correspond to the $V_{\text{TR}}$ change in voltage.     |
| $P_{RA}^{-1}()$  | inverse function of $P_{RA}$ predictor   |
| $\tau = P_{RA}^{-1}(P_{RB}(t_{\text{pulse}}))$                     | thermal response time constant   |

Note:  $t_A, \Delta t_A, t_B, \Delta t_B, t_{\text{TR}}$  are programmable values. Please refer to Figure A.

Default settings:

|                         |                                 |                                  |
|-------------------------|---------------------------------|----------------------------------|
| $t_A = 72.5\mu\text{S}$ | $\Delta t_A = 145\mu\text{S}$   | $t_{\text{TR}} = 100\mu\text{S}$ |
| $t_B = 0\mu\text{S}$    | $\Delta t_B = 362.5\mu\text{S}$ |                                  |

### 3. Heat Model Analysis

| Symbol/Equation   | Description                                      |
|---|--|
| $\alpha_{BW}$   | bridgewire temperature resistance coefficient    |
| $\Theta = \frac{1}{\alpha_{BW}} \cdot \frac{\Delta R}{R_0}$                 | final bridgewire temperature offset from ambient |
| $\overline{PA} = [P_{IA}(t_{\text{AMID}})]^2 \cdot P_{RA}(t_{\text{AMID}})$ | average dissipated power over range $R_A$        |
| Slope( $P_{RA}$ ), Slope( $P_{RB}$ )  | $P_{RA}$ and $P_{RB}$ predictor slopes           |

(continued on next page)

$$C_p = \frac{E_A}{\Delta T_A} = \frac{\overline{P_A} \cdot \Delta t_A}{\frac{\Delta R_A}{R_0} \cdot \frac{1}{\alpha_{BW}}} = \overline{P_A} \cdot R_0 \cdot \alpha_{BW} \cdot \frac{\Delta t_A}{\Delta R_A} = \alpha_{BW} \frac{\overline{P_A} \cdot R_0}{Slope(P_{RA})}$$

$C_p$  of the bridgewire

$$\overline{P_B} = \frac{E_B}{\Delta t_B} = \frac{C_p \Delta T_B}{\Delta t_B} = CP \frac{1}{\Delta t_B} \cdot \frac{\Delta R_B}{R_0} = \frac{C_p}{\alpha_{BW} \cdot R_0} Slope(P_{RB})$$

average dissipated power over range  $R_A$

$$\gamma = \frac{\overline{P_A} - \overline{P_B}}{\Theta} \quad \text{thermal conductance in } \left[ \frac{Watts}{deg C} \right]$$

$$IF_n, \quad \left( \frac{dIF}{dt} \right)_n \quad \text{filtered } I_n \text{ and } \left( \frac{dI_n}{dt} \right)_n, \text{ respectively}$$

$$RF_n, \quad \left( \frac{dRF}{dt} \right)_n \quad \text{filtered } R_n \text{ and } \left( \frac{dR_n}{dt} \right)_n, \text{ respectively}$$

$$T_n = \left( \frac{RF_n}{R_0} - 1 \right) \cdot \frac{1}{\alpha_{BW}} \quad \left( \frac{dT}{dt} \right)_n = \frac{\left( \frac{dRF_n}{dt} \right)_n}{R_0} \cdot \frac{1}{\alpha_{BW}}$$

bridgewire temperature

$$P_n = IF_n^2 \cdot RF_n \quad \text{total dissipated power}$$

$$Cp_n = \frac{E_n}{\Delta T_n} = \frac{Pn}{\frac{\Delta T_n}{\Delta t_n}} = \left( \frac{dT}{dt} \right)_n \quad \text{instant } C_p \text{ of the bridgewire}$$

$$P_{BW_n} = \frac{E_{BW_n}}{\Delta T_n} = \frac{CPn \cdot \Delta T_n}{\Delta T_n} = CP_n \cdot \left( \frac{dT}{dt_n} \right)_n \quad \text{power consumed on heating the bridgewire proper}$$

$$P_{PH_n} = P_n - P_{BW_n} \quad \text{power dissipated into the rest of the structures}$$

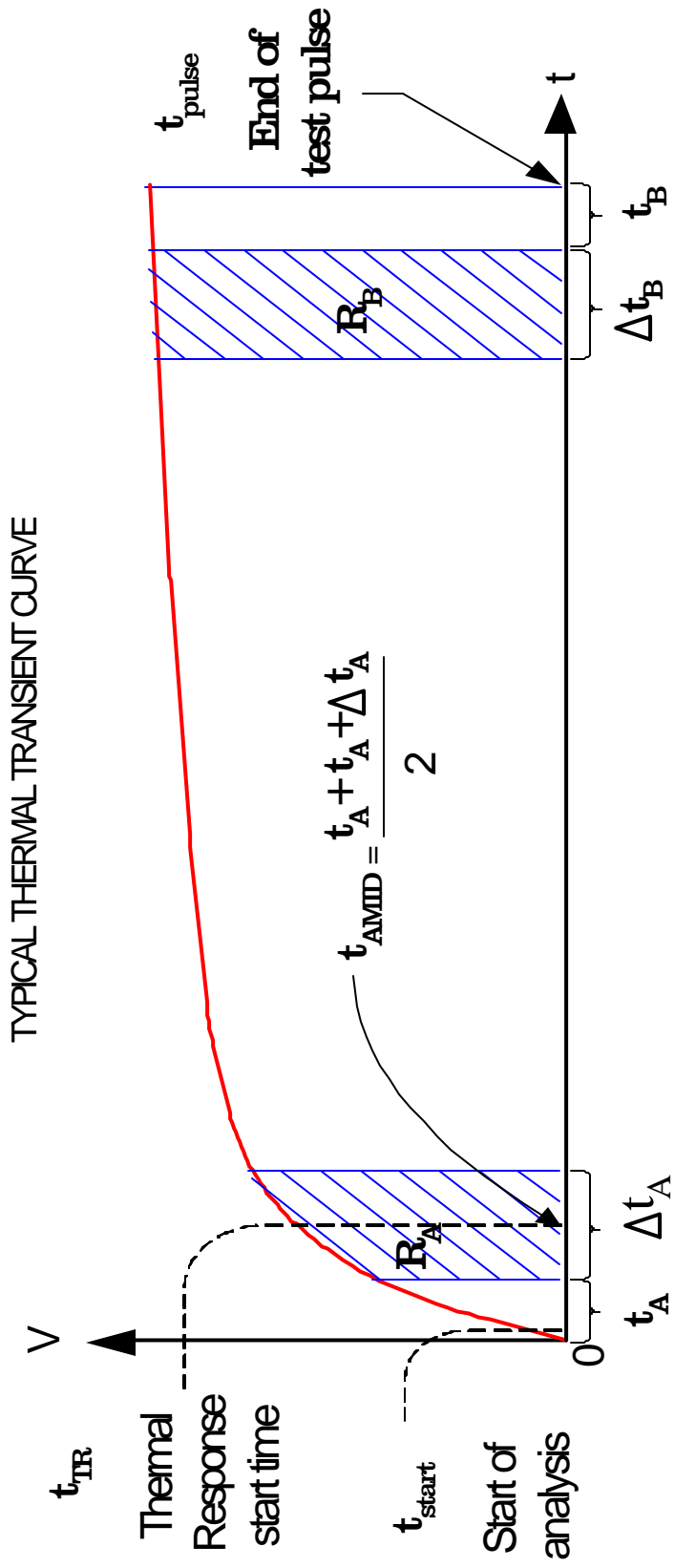


Figure A. Thermal Response Curve Timing